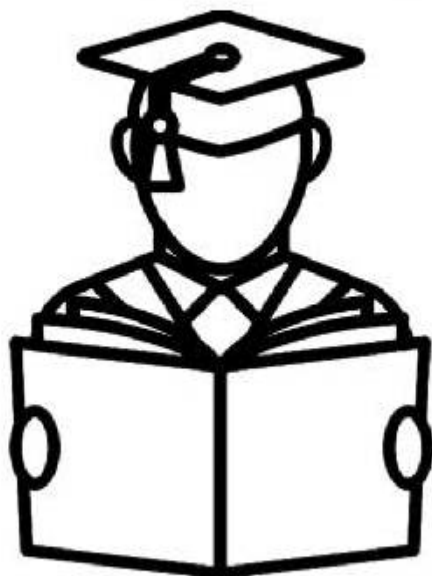


चौधरी PHOTOSTAT

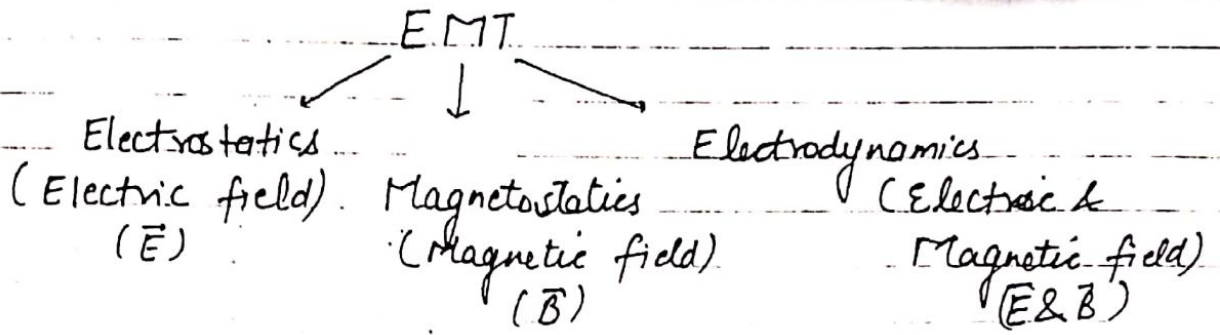
"I don't love studying. I hate studying. I like learning. Learning is beautiful."



"An investment in knowledge pays the best interest."

Hi, My Name is

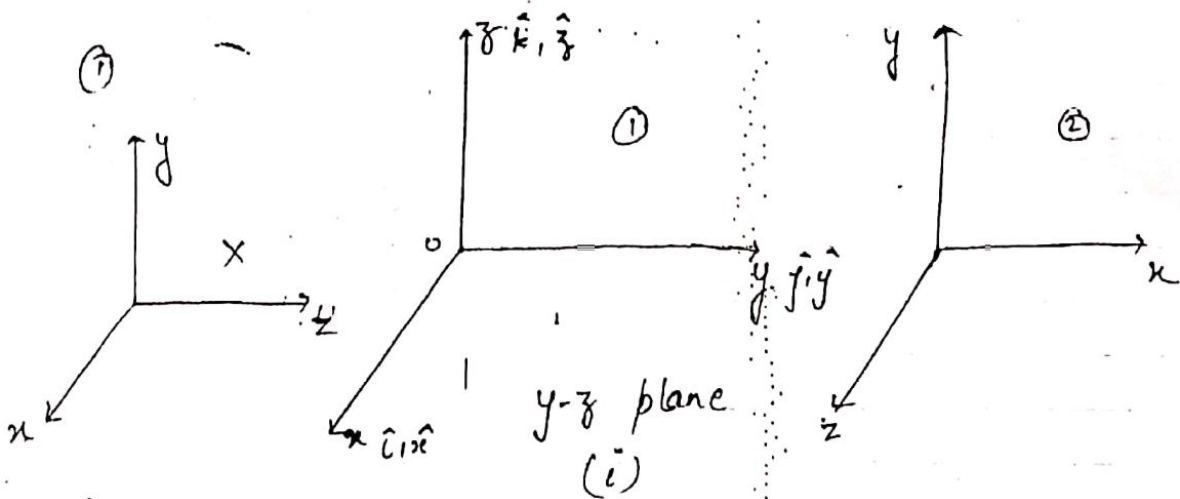
Physical Science
for CSIR NET
Career Endeavour



Mathematics required for EMT

Co-ordinate Systems:

- ① Cartesian system
- ② Spherical polar system
- ③ Cylindrical system



$$\hat{i} \times \hat{j} = \hat{k}$$

$$\hat{i} \times \hat{k} = -\hat{j}$$

length elements of (i)

$$d\vec{r} = dx \hat{i}, \quad d\vec{y} = dy \hat{j}, \quad d\vec{z} = dz \hat{k}$$

along OA line

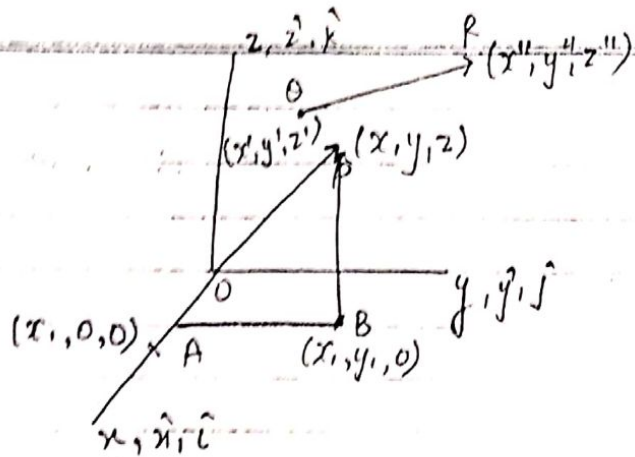
$$\int_0^{x_1} f(x, y, z) dx \Big|_{\substack{y=z=0 \\ z=0}}$$

along AB line

$$\int_0^{y_1} f(x, y, z) dy \Big|_{\substack{x=x_1 \\ z=0}}$$

along BP line

$$\int_0^{z_1} f(x, y, z) dz \Big|_{\substack{x=x_1 \\ y=y_1}}$$



$$d\vec{l} = dx \hat{i} + dy \hat{j} + dz \hat{k}$$

$$\vec{OP} = (x-0)\hat{i} + (y-0)\hat{j} + (z-0)\hat{k}$$

$$\vec{QR} = (x''-x_1)\hat{i} + (y''-y_1)\hat{j} + (z''-z_1)\hat{k}$$

Surface elements (plane):

$$d\vec{S} = d\vec{y} \times d\vec{z}$$

$$d\vec{S} = \underbrace{dy dz}_{\text{magnitude}} \hat{i} \quad \text{dis?}$$

Whatever vector is constant over the surface that will the direction of that surface and here y & z is vary and x is constant. So \hat{i} is dirⁿ.

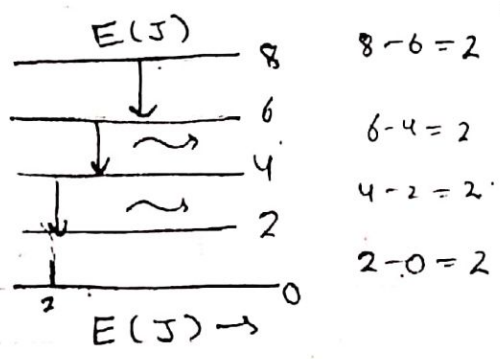
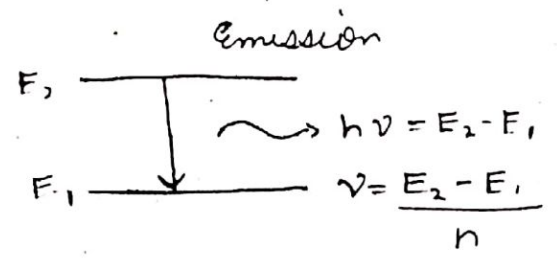
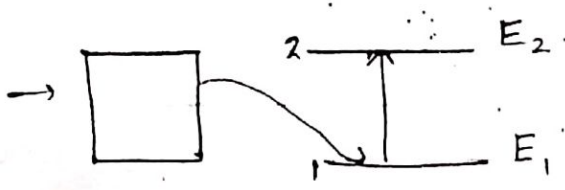
Atomic & Molecular Physics

Spectroscopy is the interaction b/w E.M. radiation and the substance to be examined.

Absorption spectra

Sample → energy is less initially

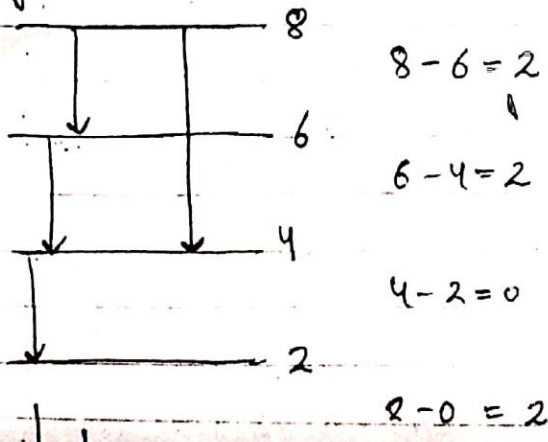
I.R → vibration, V.V → e⁻ released



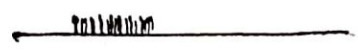
difference = peak
4-2 = 2

all are having difference same i.e 2 so we get only one peak at 2 instead of 3 different peaks.

At some time one atom is present at one level only. Only one transition at a time



8-4=4
two peak at 2 and at 4.



Band spectra:

Line are very closed which seems like bar

E(J) → 2 4 line spectra

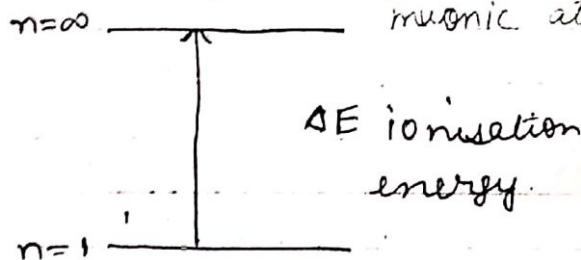
Hydrogen atom:

atom \rightarrow +ve charge nucleus } electrically
 \rightarrow -vely charged e^- s. } neutral

Atomic no. \rightarrow no. of protons.

Bohr's theory of H-like atoms

This theory is applicable for $1e^-$ system like hydrogen (H), He^+ , Li^{2+} , Be^{3+} positronium, muonic atom



Assumptions

1. Electrons are revolving in circular orbits around the nucleus.
2. Electrons move only in those orbits in which orbital angular momentum is integral multiple of \hbar .

$$m v r = n \hbar \quad n = 1, 2, 3, \dots, \infty$$

or

$$m v_n r_n = \frac{n h}{2\pi}$$



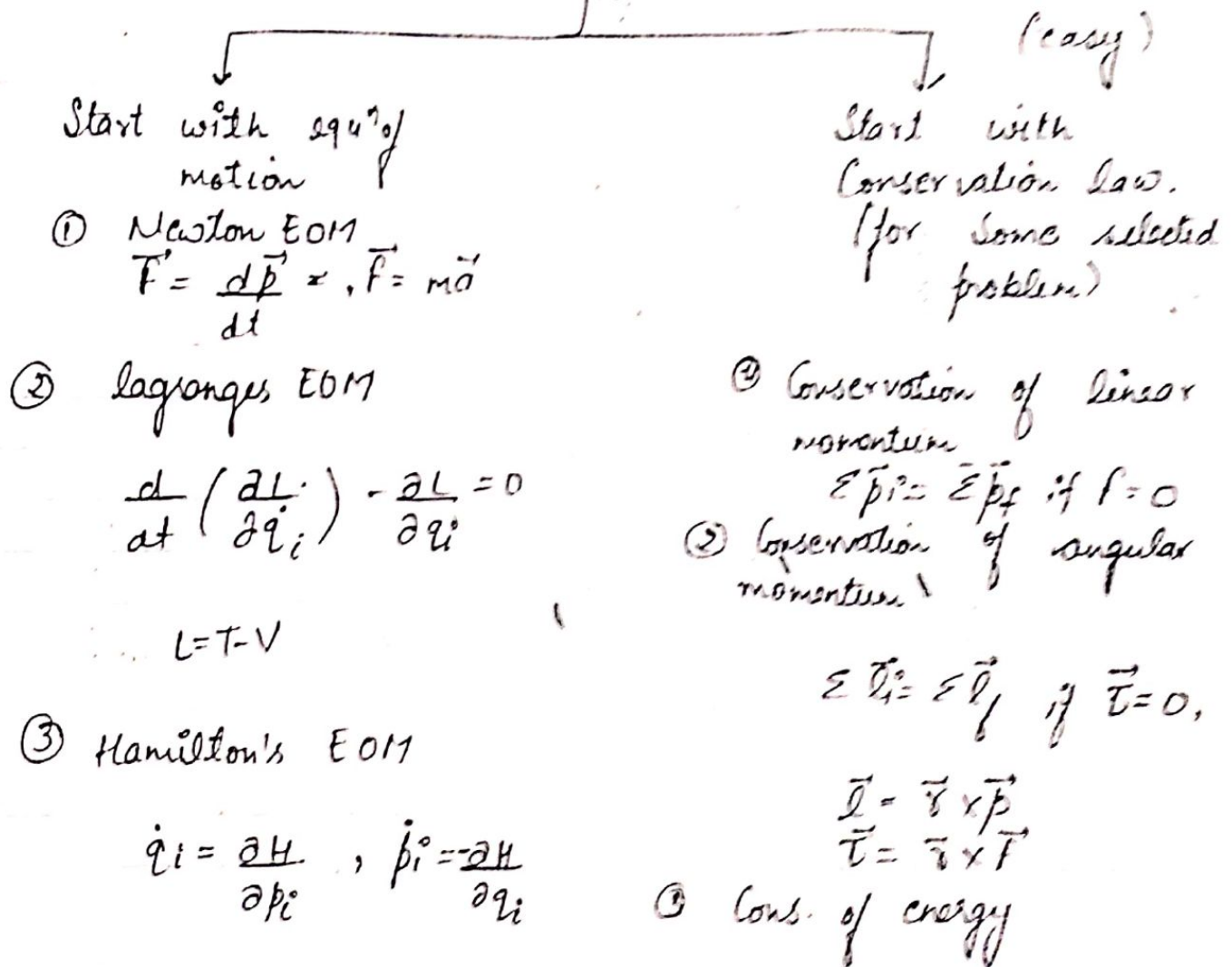
Proof:- $2\pi r = n \lambda$

e^- move as wave having wavelength λ
& this wave should have integral no. of wavelengths.

Newtonian Mechanics.

General approach for solving problem

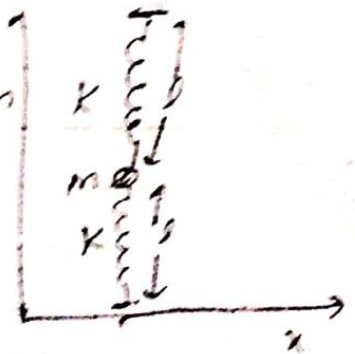
Two approaches



Example NET-2013 (5M)

If block is slightly displaced in x-dir then write its eqn of motion.

This Ques. can be solved by four methods



~~If only spring is attached, then @ is conserved no other force applied.~~

Newtonian Mechanics

Basic assumption: Mass, length and time are absolute. These quantities do not change.

Newton's laws:

2nd law - $\vec{F} = \frac{d\vec{p}}{dt}$

Rate of change of momentum of the system is equal to net applied force.

$$\frac{d\vec{p}}{dt} = \frac{d}{dt}(m\vec{v})$$

Total mass never change.

$$\frac{d\vec{p}}{dt} = m \frac{d\vec{v}}{dt} + \vec{v} \frac{dm}{dt}$$

Above formula is used for both constant and variable mass.

If $m = \text{constant}$

$$\vec{F} = m \frac{d\vec{v}}{dt} = m\vec{a}$$

$$\because \vec{a} = \frac{d\vec{v}}{dt}$$

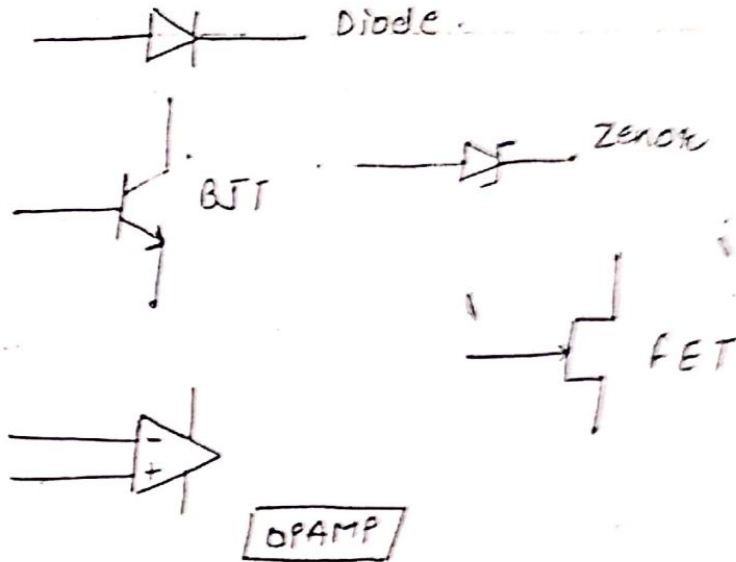
used only if mass is constant

$$\boxed{\vec{F} = m\vec{a}}$$

This force is obtained when we are assuming mass is constant.

acceleration is zero only when velocity is constant.

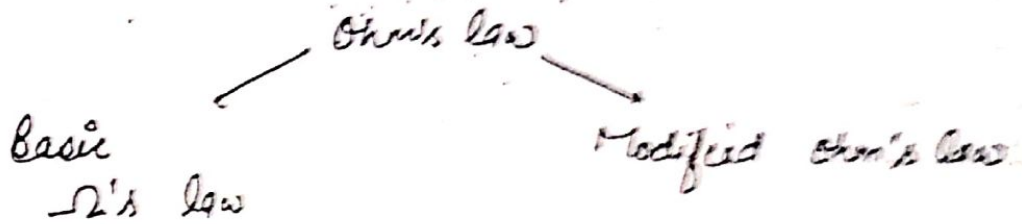
Analog



Network theory

Resistor → Resistance is a property of resistor which opposes the flow of current.

Its behaviour is explained by Ohm's law



OR.
Field theory
Ohm's law
 $J \propto E$
 $J = \sigma E$

$\sigma \rightarrow$ Conductivity

OR
Circuit theory Ohm's law

V & I: $V = R \cdot I$

I & V: $I = G \cdot V$

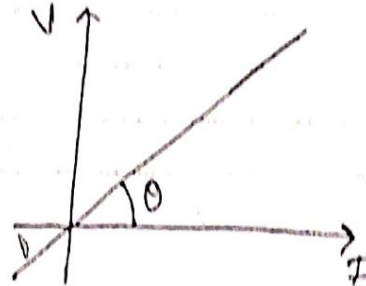
$R = \frac{V}{I} \Rightarrow \frac{\text{Volt}}{\text{ampere}} = \frac{\Omega}{\Omega}$

Teacher's Signature _____
 $G \rightarrow$ Conductance

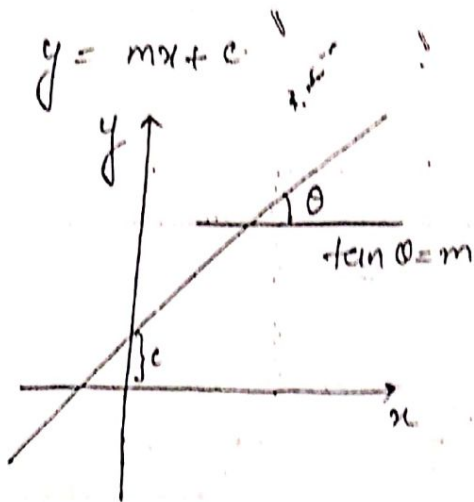
$$G = \frac{I}{V}$$

$$\text{AHO} = \frac{\text{ampere}}{\text{volt}} = \text{ohm}^{-1}$$

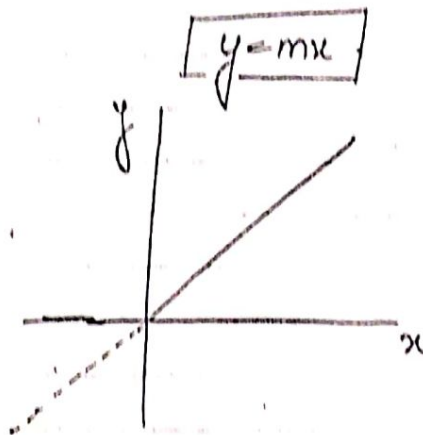
graph b/w V and I



$$\tan \theta = m = R_{ohm}$$

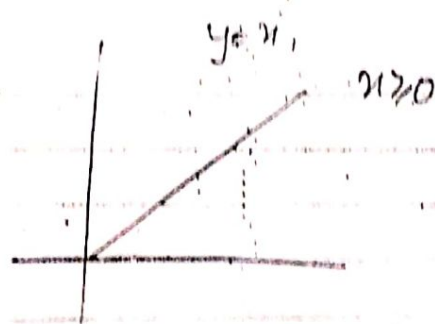


Non linear characteristics



linear characteristics

at $x=0 = c$ initial value for constant



Non-linear characteristics / curve

Mathematical Physics

Part 1

Complex Analysis

Basic preview of Complex Variable.

$$az^2 + bz + c = 0$$

$$z \Rightarrow \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$b^2 - 4ac > 0 \quad \checkmark \quad (+ve)$$

$$b^2 - 4ac < 0 \quad (-ve)$$

$$\sqrt{-1} = i$$

$$i^2 = -1$$

$$z = x + iy \quad (\text{CARTESIAN FORM})$$

$x \rightarrow$ real part

$y \rightarrow$ imaginary part

Electric field.

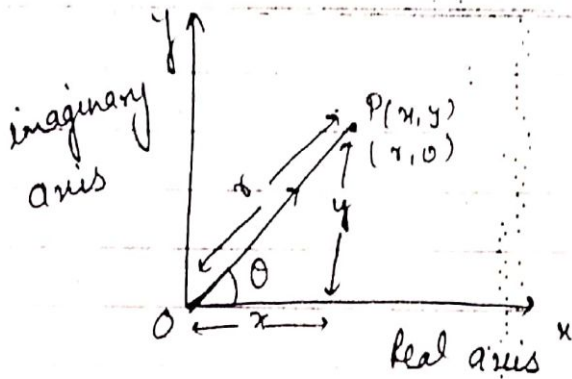
$$\vec{E} = \vec{E}_0 \cos(kz - \omega t)$$

$$\{\cos\theta + i\sin\theta\}$$

$$\vec{E} = \vec{E}_0 \left[\text{Real part of } e^{i(kz - \omega t)} \right]$$

$$\begin{aligned} \{\text{Polar form}\} \quad z &= r \cos\theta + ri \sin\theta \\ &= r (\cos\theta + i \sin\theta) \\ &= r e^{i\theta} \end{aligned}$$

\Rightarrow Geometrical Representation of a Complex Number
Complex Argand Plane.



\vec{OP} = radius vector corresponding to the complex no. z
 $r \rightarrow$ length / Magnitude of the radius vector OP
 \rightarrow modulus of the 'z'

$$\Rightarrow r = |z| = \sqrt{x^2 + y^2} = \sqrt{(R.P.)^2 + (I.P.)^2} =$$

$\Rightarrow \theta =$ angle which radius vector \vec{OP} makes with
 +ve x-axis
 $=$ argument of $z =$ Phase of z

$$\theta = \arg. z = \tan^{-1}\left(\frac{y}{x}\right)$$

$$\theta = \tan^{-1}\left(\frac{I.P.}{R.P.}\right) = \text{Phase}$$

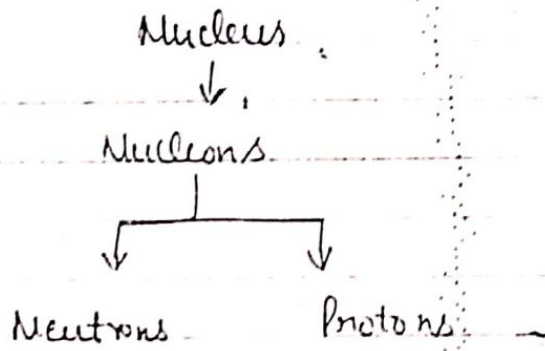
Important Relⁿ regarding argument z and modulus.

$$(1) |z_1 + z_2| \leq |z_1| + |z_2|$$

$$(2) |z_1 - z_2| \geq |z_1| - |z_2|$$

$$(3) |z_1 \cdot z_2| = |z_1| \cdot |z_2|$$

$$(4) \left| \frac{z_1}{z_2} \right| = \frac{|z_1|}{|z_2|}$$



Z^A A = mass number (no. of n & p)
 z = atomic number (no. of p)

Masses - Can be expressed in

- kg
- Atomic mass unit (amu) or u
- Relativistic unit (MeV/c²)

	kg	u	MeV/c ²
Proton	1.6726×10^{-27}	1.00726 u	938.3
Neutron	1.6750×10^{-27}	1.00867 u	939.6
Electron	9.1×10^{-31} kg	0.00055 u	0.51

Atomic mass unit (amu)

1 amu = $\frac{1}{12}$ time the mass of one C^{12} atom

1 mole of C^{12} = 12 gm

1 mole has = 6.02×10^{23} atoms

Mass of one C^{12} atom = $\frac{12}{6.02 \times 10^{23}}$ gm

$$1 \text{ amu} = \frac{1}{12} \times \frac{12}{6.02 \times 10^{23}} \text{ gm} \times 10^{-3} \text{ kg}$$

$$1 \text{ amu} = 1.66 \times 10^{-27} \text{ kg}$$

1 amu in energy units

$$E = mc^2 = 1 \text{ amu} \times c^2$$

$$E = 1.66 \times 10^{-27} \text{ kg} \times (3 \times 10^8 \text{ m/s})^2 = \text{Joule}$$

$$1 \text{ J} = \frac{1}{1.6 \times 10^{-19}} \text{ eV}$$

large \uparrow small \uparrow magnitude must be large

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

$$1 \text{ MeV} = 1.6 \times 10^{-19} \times 10^6 \text{ J}$$

$$1 \text{ MeV} = 1.6 \times 10^{-13} \text{ J}$$

$$E = 1.66 \times 10^{-27} \times (3 \times 10^8)^2 \text{ J}$$

$$1.5 \times 10^{-13} \text{ J/MeV}$$

Quantum Mechanics

	Q/ Marks	Q/ Marks	
CSIR	4x3.5	4x5	= 34 Marks
Gate	4x1	4x2	= 8 Marks + 4 Marks = 12 Marks

⇒ Total @ of a material particle in relativistic case

$$E = mc^2 = \gamma mc^2, \quad E = K \cdot E + m_0 c^2 \quad (v \sim c)$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$E = \sqrt{c^2 p^2 + m_0^2 c^4}$$

⇒ For non-relativistic free particle.

$$E = K \cdot E = \frac{1}{2} m v^2$$

($v \ll c$)

non-relativistic

$v \ll c$ non-rel. ($\gamma = 1$)

$v \sim c$ rel. ($\gamma > 1$)

$v = 10^8 \text{ m/sec}$

$v = 10^8, v = 2 \times 10^7$

$$\gamma = \frac{1}{\sqrt{1 - \frac{10^{12}}{9 \times 10^{16}}}} = \frac{1}{\sqrt{\frac{9 \times 10^{16} - 10^{12}}{9 \times 10^{16}}}} = \frac{1}{\sqrt{1 - 0.11 \times 10^{-4}}} = \frac{1}{\sqrt{0.99 \times 10^{-4}}}$$

$\boxed{\gamma = 1.0001}$

$v = 2 \times 10^7$

$$\gamma = \frac{1}{\sqrt{1 - \left(\frac{2 \times 10^7}{3 \times 10^8}\right)^2}}$$

$\boxed{\gamma = 1.002}$

$E = cp = h \nu$

If $v < 10^7 \text{ m/sec}$ (non-relativistic)

$v > 10^7 \text{ m/sec}$ (relativistic)

$$\textcircled{1} \int_0^{\infty} e^{-\lambda x} x^n dx = \frac{n!}{\lambda^{n+1}}$$

$$\textcircled{2} \int_0^{\infty} e^{-\lambda x} x^n dx = \frac{n!}{\lambda^{n+1}} = \frac{(n+1)!}{\lambda^{n+1}}$$

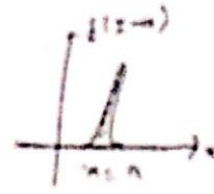
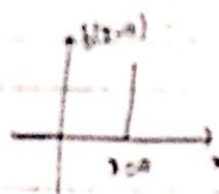
$$\textcircled{3} \int_0^{\infty} e^{-\lambda x^2} x^n dx = \frac{\sqrt{\pi}}{2\lambda} \frac{\Gamma(\frac{n+1}{2})}{\lambda^{\frac{n+1}{2}}}$$

$$\textcircled{4} \int_{-\infty}^{\infty} e^{-\lambda x^2 + \beta x} dx = \sqrt{\frac{\pi}{\lambda}} e^{\frac{\beta^2}{4\lambda}}$$

$$\textcircled{5} \int_{-\infty}^{\infty} f(x) dx = \begin{cases} 2 \int_0^{\infty} f(x) dx, & \text{if } f(x) = f(-x) \\ & f(x) = \text{even} \\ 0, & \text{if } f(x) = -f(-x) \\ & f(x) = \text{odd} \end{cases}$$

Dirac Delta

$$\delta(x-a) = \begin{cases} 0 & x \neq a \\ \infty & x = a \end{cases}$$



$$\psi(x) = \frac{1}{\sqrt{2\pi a^3}} e^{-\frac{(x-a)^2}{2a^3}}$$

Then is only single value of position $x=a$ where

$$\langle x \rangle = a, \quad \langle x^2 \rangle = a^2$$

$$\Delta x = \sqrt{\langle x^2 \rangle - \langle x \rangle^2} = 0$$

relativistic energy $E = \gamma mc^2 = \frac{hc}{\lambda} = cp$

total @ of rel. free particles

$$E = \sqrt{(cp)^2 + (mc^2)^2}$$

$$= K.E + mc^2$$

$$E = \gamma mc^2$$

Comparison of rel. & non-rel.

$v \ll c, v < 10^8 \text{ m/sec.}$ } non-rel.
 $v \ll 1$
 rel. mass \approx rest mass

$v \approx c, v > 10^8 \text{ m/sec.}$ } rel.
 $\gamma > 1$
 rel. mass \neq rest mass

$cp \ll mc^2$ } non-rel.
 $cp \approx mc^2$ } rel.
 or $cp > mc^2$

$K.E. \ll mc^2$ } non-rel.
 $K.E. = mc^2$ } rel.
 $K.E. > mc^2$

For free particles

$$mc^2 = 0.511 \text{ MeV}$$

$$mc^2 = 938.25 \text{ MeV}$$

$$mc^2 = 931.5 \text{ MeV}$$

Lecture - 1

Solid state Physics

NET → Marks ⇒ $5 \times 3 = 15 + 3.5 = 18.5$

Questions

15-20

GATE → Marks contribution: 9-10

- Books ⇒
1. Kittel ✓
 2. Puri and Bahari ✓
 3. Wajahat
 4. Ali Omar
 5. Ascroft & Hemmings
 6. Lim - series

We will study the properties of Solid (Physical)

Physical properties of solid depends upon crystal structure.

For this, we take a lattice

Lattice

* consider a atom as a hard sphere



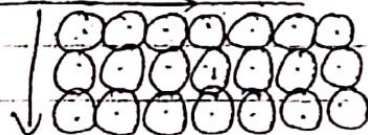
r → radius of atom

Solid is composed of millions atoms.

• if atom in solid not arranged periodically then it is non-crystalline solid

• if they are arranged periodically then it is crystalline solid


eg
diamond
quartz

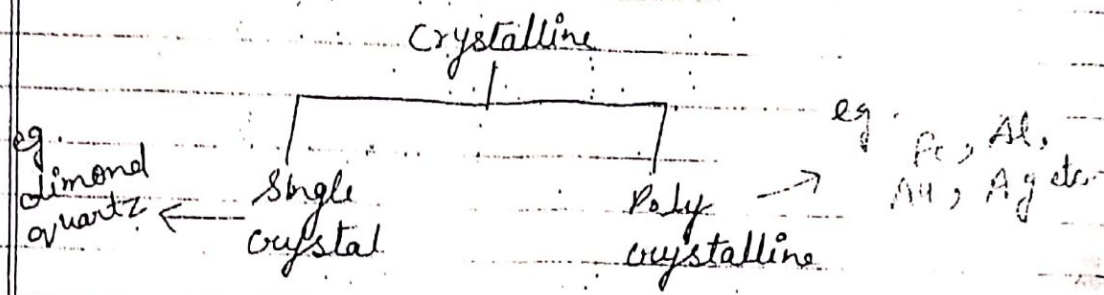


(It 2-d i.e. a plane)

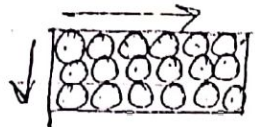
if you place one layer of atom on this it become atomic plane.

if one more than it become 3-d.

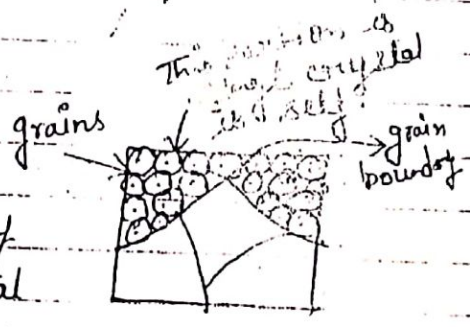
eg.  Non-Crystalline (randomly arranged)
glass, rubber



• If there is no break in the arrangement of solid atoms then it is single crystal.



• Poly Crystalline solids are considered as aggregate of large no. of single crystal

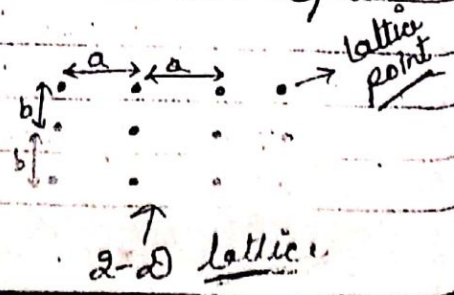


if we break poly crystal it will break through grain boundary.

We will study the periodic arranged crystals solids.

Lattice :- Lattice is periodic arrangement of imaginary points in the space.

if we consider these points in space then distance b/w them will be same.



Thermodynamics :

↓
Macroscopic
approach
↓

Statistical Mechanics ①

↓
Microscopic approach.

Microscopic Parameter or Variable:

The parameters related to the constituents of the system are called microscopic parameter.

Macroscopic Parameter:

The parameters related to the system as a whole are called macroscopic parameter.

P, V, T, U, S, G

* Pressure is net momentum transfer per unit time per unit area.

* The state related to the parameters of the system is called macroscopic state or macro state.

* The state related to the parameters of the constituents of the system is called microstate or microscopic state.

System & Surrounding :

* The portion of universe of a particular mass in which observer is interested is called System.

* The part of the universe that is exterior to the system and influence or affect the system or ~~affect~~ interact with

Surroundings or environment.

3

$$\text{System} + \text{Surrounding} = \text{Universe}$$

★ Depending on the interaction of system and surrounding, systems are classified as follows.

Open System

→ A system that can exchange energy as well as matter (rest mass energy) with its surrounding is called open system. (excluding rest mass energy)

Ex Ocean is open system. Sun is acting as surrounding.

Ex Most part of universe is open system.

Closed System

→ A system that can exchange energy but not matter with its surrounding is called closed system.

Isolated System

A system that can not exchange energy as well as matter with its surrounding is called isolated system.

- NO real system is absolute isolate.
- Universe is example of isolated system.

Closed & isolated ~~the~~ ~~these~~ systems can be called as bodies.